Modeling and Simulations of Lüneburg Lens Antennas for Communication Purposes

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Abstract — The paper is dealing with the principles for modeling and simulating by 3D simulators of the well-known Lüneburg lenses used as communication antenna devices. The models of spherical, semi-spherical and cylindrical multi-layer dielectric lenses are discussed. The results show the effectiveness of the proposed simulation procedures for investigation of the focusing effects and antenna parameters of these large-scale beam-forming devices.

Keywords — antennas, dielectric antennas, electromagnetic 3D simulators, focusing, lens antennas.

I. INTRODUCTION AND BASIC MODEL

The Lüneburg lens is historically connected with the possibilities of transforming the plane wave into a point-like spherical wave or vice versa [1]. Considered as an antenna, if the Lüneburg lens is illuminated by a plane wave from a remote source – satellite or HAP (High-Altitude Platform) antenna, the wave front will be focused into a small receiving horn/patch (or v. v.), acting like an antenna array with relatively high gain, small main-lobe beam-width and low-level side lobes. Nowadays there is a great interest in such type of antennas for applications in the modern mobile communications [2], radioastronomy [3], etc. Moreover, the Lüneburg lenses at the moment are considered as the simplest and the cheapest passive antennas for communication purposes [4]. The big Lüneburg lenses have an advantage related to the phase antenna arrays, because they can simultaneously collect signals from all directions (multi-beam option). Other serious advantage is the broadband operation. These lens antennas can be manufactured with inexpensive dielectric materials and without any active elements. Their main disadvantages are the large size, the relatively big dielectric loss and the fabrication complexity.

The focusing action of the classical Lüneburg lens is based on the gradient distribution of the refraction index \( n(r) \) or the relative dielectric constant \( \varepsilon_r \) into a sphere with radius \( R \). The fundamental expression is:

\[
\varepsilon_r(r) = \frac{2 - (r/R)^2}{2} \quad \text{or} \quad \varepsilon_r(r) = 2 - (r/R)^2
\]

According to (1) the dielectric constant near to the outer sphere surface should be \( \varepsilon_r = 1 \) (air), while in the centre of the sphere \( \varepsilon_r = 2 \) (Fig. 1). This distribution is not easy to be exactly realized. The practical realization utilizes step-recovery distribution in \( N \) layers with regular or irregular width (or the radius of the corresponding coaxial sphere).

Therefore, the lens focusing action depends first of all on the ability to construct the necessary distribution of the dielectric constant in the sphere volume. We can classify two main methods for construction of materials with accurately assigned values of the dielectric constant: i) by dielectric mixtures [4] and ii) by mechanically inserted air-filled holes into plane slices of homogeneous plastic material with relatively small dielectric constant (2.1-2.5) [5].

The simplest design of Lüneburg lens with appropriate dimensions for a given frequency range is based on the physical optics [6] and the well-known ray-tracing model. The diameter of the spherical lens should be chosen to be more than \( 10\lambda \) (\( \lambda \) – the wavelength in the considered structure at the operation frequency). This fact shows that the Lüneburg lens is an electrically big structure and, therefore, it is very difficult to be precisely simulated by electromagnetic FEM- or FDTD-based simulators. For example, the L-band lenses are with diameter ~5-10 m, Ku-band lenses – 20-25 cm, 30-40-GHz lenses – 10-15 cm, 300-GHz lenses – 20 mm. In this paper we present our experience to simulate big Lüneburg lenses by 3D electromagnetic simulators (e.g. Ansoft® HFSS-8 and 11 [7]). We investigate the focusing effect in different lens structures with a different number of layers and shapes; consider the parasitic resonance effects and the influence of the dielectric anisotropy. Finally, the main antenna parameters: gain and radiation patterns, are determined by simulations.

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II. INVESTIGATION OF THE FOCUSING EFFECTS

A. Modeling of Lüneburg lenses by 3D simulators

The classical 3D model should consist of the multi-layer focusing lens, the small-aperture illuminator (horn, planar patch, etc.) and a “radiation box”, which should ensure enough “room” for calculating the scattering fields around the antenna (see Fig. 12 in §IV). The last circumstance is very important for successful simulations, but the big dimensions of the structure do not allow fast and accurate preliminary design of the lenses. Therefore, we propose a different 3D model for effective Lüneburg lens design: lens body, rectangular \( (2R\times2R) \) planar source of plane wave, illuminating the whole lens and a PML (Perfectly-Matched-Layer) box to put the structure in – Fig. 2. Calculating the E-field distribution, we can determine the places, where the plane wave will be focused – the primary and high-order focuses outside the dielectric sphere.

Fig. 2. Illustration of the splitting of the simulated Lüneburg lens: a) full-sphere structure with dimensions 230x230x230 mm (the high-order focuses are not considered); b) once splitted structure (1/2 from the whole volume); c) twice splitted structure (1/4 from the whole volume); no more symmetrical splitting is possible!

B. Resonance effects at low frequencies

The Lüneburg lens antenna is in principle a broadband device. In fact, the frequency bandwidth is restricted from below, due to the influence of the parasitic low-frequency resonances on the focusing effect. The model proposed here for simulation allows to easily obtain the resonance frequencies of the first low-order resonances of the sphere (see Fig. 5). Our investigations show that the practical low-frequency limit of the Lüneburg lens antenna for well enough focusing is \( f_L \sim (2-3)f_1 \), where \( f_1 \) is the lowest-order resonance frequency of the dielectric sphere.

Fig. 3. Focusing abilities of 200-mm Lüneburg lens with different number \( N \) of layers (\( f = 3.5 \) GHz): the focusing effect becomes worse, when \( N \leq 2-4 \) (log scale)

C. Frequency dependence of the focusing effect

Now we can step in the next stage of the lens design – to investigate the focusing effect versus the frequency. We concentrate our attention to determine the position of the first focus outside the sphere; the high-order focuses are not interesting for antenna applications. We apply everywhere the simplest quarter-split model (Fig. 4c). Realistic simulations are possible up to \( f \sim (10-15)f_1 \); above \( \sim 15f_1 \) the computational platform used should have enough RAM memory (e.g. > 4 GB). Fig. 6 presents the frequency behavior of the focusing effect in 200-mm Lüneburg lens. We can trace the evolution of the position of the focuses (the spots with E-field maximums) with the decreasing of the wavelength. The first outside focus is well defined at high frequencies. The number of inside focuses (into the sphere) increases with the frequency. Contrariwise, no outside focuses exist at the resonances and destroying of the focusing effect is detected near to the low-frequency resonances. Thus, the frequency bandwidth of the Lüneburg lens can be estimated, for example, between \( f_L \sim 5f_1 \) up to very high frequencies, when separate layers might act like single resonators. At very high frequency we observe additional outside focuses near to the primary focus, but they could be minimized by optimization of the multilayer distribution.
D. Optimization of the multi-layer distribution

Fig. 7 demonstrates again the focusing effect by spheres with different number of layers, but at a relatively high frequency ($f = 10$ GHz for a sphere with $R = 100$ mm). Now the focusing effect is more clearly expressed and we can observe new effects in dependence of the number of layers used in the model ($N = 10, 5, 4, 3, 2$). If the lens has $N = 10$ regular layers, the primary focus outside the sphere volume is close to the sphere surface at a distance $a \sim 5$ mm. In the case of $N = 5$ this distance becomes bigger, $a \sim 7$ mm and for $N = 4, a \sim 9$ mm (i.e. the primary focus spot moves away from the surface and the focusing effect becomes weaker). Further, in the case of $N = 3, 2$ the considered first focus outside the lens volume is already not well defined (the E-field level is weaker). Therefore, we can conclude, that $N = 5-10$ of the layers number are optimal enough to construct a well-focusing Lüneburg lens antenna for communication purposes.

E. Effect of the anisotropy of the dielectric layers

The last problem, which we have to check, is the influence of the possible anisotropy of the dielectric constant over the focusing effect. We find out that anisotropy is important, if it leads to a change of the needed dielectric-constant distribution of the sphere lens. Thus, layers with big anisotropy may destroy the focusing action of the sphere as a Lüneburg lens – Fig. 9c.

III. LÜNEBURG LENSES OF DIFFERENT SHAPES

A. Conventional spherical lens

The spherical Lüneburg lens is a classical antenna element, which focus is at the opposite end of the incoming wave. Up to now, we have investigated only this type of lenses. However, other more effective types of lenses can be utilized for communication purposes.

B. Semi-spherical lens

One of the most suitable antennas for satellite communications is the semi-spherical Lüneburg lens with a flat, metalized bottom surface. In this case the primary focus is placed at 90° according to the direction of the incoming from the satellite signal [2]. This lens ensures more reliable mechanical constructions for steerable satellite or HAP antennas. Fig. 10 shows the focusing effect in a simulated semi-spherical Lüneburg lens with 5 irregular layers. Now we simulate a half part of the semi-sphere, but the simula-
tions are less efficient due to reflections. We observe good focusing effect in both directions of polarization – normal (E field of the plane wave is perpendicular to the metal screen) and parallel (E field is parallel to the metal screen). This is very important for the realization of dual-polarization satellite antennas.

C. Cylindrical lens

An interesting and fully applicable cylindrical Lüneburg lens is shown in Fig. 11. It is similar to the semi-spherical lens, but it is constructed by irregular coaxial cylindrical layers. The specific peculiarity of this lens is the shape of the focus spot as a long thin tape along the cylinder axis.

IV. SIMULATION OF THE ANTENNA PARAMETERS

The presented preliminary design of the Lüneburg lens, based on the focusing effect, can give the optimal value of the sphere diameter for the chosen frequency range, the lens shape and focus position, the optimized distribution of the layers, etc., but cannot give the antenna parameters – radiation patterns, gain, efficiency, etc. Besides, the interaction between the illuminating horn and the whole antenna is not known.

Therefore, we can finish the design procedure with simulations of the realistic structure: the whole lens and the illuminating source. The antenna source – open-end cylindrical waveguide, horn or planar patch, might be separately optimized for the frequency range of interest. In fact, the matching of the Lüneburg lens antenna, the restrictions in the operation bandwidth and even the cross-polarization level depend mainly on the horn properties. We use in this paper a simple cylindrical open-end waveguide with a narrow frequency band around 10 GHz, set at distance 5 mm to the lens surface with elevation angle $45^\circ$. The aim is to construct a reasonable 3D model of the whole antenna: semi-spherical 8-layer lens and a simple source – Fig. 12a.

First, we started simulations of the S-parameters with a split model of the hemi-sphere. The radiation-pattern diagram is presented in Fig. 13a. Then we repeated the simulations again with a model of the whole semi-sphere – the results are given in Fig. 13b. We shall note, that the presented radiation diagrams practically coincide for both of the models. The only difference is the cross-polarization level: $-35$ dB for the whole hemi-sphere versus an unrealistic value $-90$ dB for the splitted lens (the cross-polarization level in the exciting source is neglected here). The side-lobe level of the diagram is about $-20$ dB. The calculated gain is about 25 dBi for both polarizations. This value depends mainly on the lens diameter; it increases with the increasing of the diameter. The beam-width at 3-dB-level is $9.71^\circ$ for the normal polarization and $10.78^\circ$ for the parallel polarization.

Finally, we can conclude that the Lüneburg lens can be successfully designed and simulated by 3D simulators in spite of the relatively big dimensions of the structure. The design process can be divided in two stages: 1) a preliminary design, which includes the exposition of the splitted lens model with a plane wave in order to investigate the focusing effects and 2) final simulation of the whole optimized structure with a transmitting horn and determination of the radiation pattern and the antenna gain.

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